

[1] involute Σ iii(spur and helical gear design system)
English version

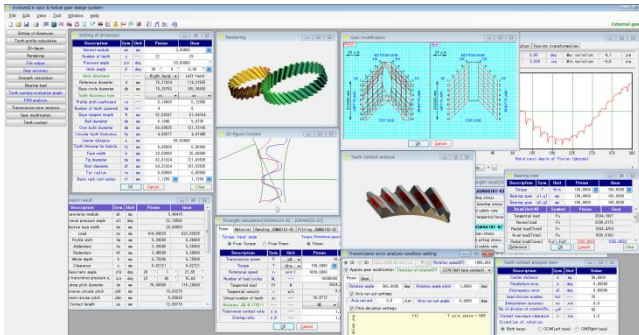


Fig.1.1 involute Σ iii(spur and helical)

1.1 Abstract

involute Σ iii (spur and helical) has functions such as cylindrical gear dimensions, strength (steel, resin), axial load, tooth surface modification, transmission error, tooth surface evaluation, FEM analysis, tooth profile data, etc. for efficient and accurate design. Fig.1.1 shows the whole screen.

1.2 Software structure

The structure of involute Σ iii is shown in Table 1.1. ○ in the table is included in the basic software, and ⊙ is optional. Applicable gear: involute spur and helical gear (external gear, internal gear)

Table 1.1 Software structure

No.	Item	Page	Structure
1	Basic rack setup	1.3	○
2	Dimension	1.4	○
3	Inference	1.5	○
4	Tooth creation drawing	1.6	○
5	Meshing drawing	1.6	○
6	Meshing rotation function	1.6	○
7	Tooth profile rendering	1.7	○
8	Gear accuracy	1.8	○
9	Gear strength calculation (steel)	1.9	○
10	Gear strength calculation (resin)	1.10	○
11	Metal × resin gear strength	1.10	○
12	Bearing load	1.11	○
13	Sliding ratio, Hertzian stress	1.12	○
14	Tooth profile output (DXF, IGES)	1.17	○
15	HELP menu	1.19	○
16	Design data management	1.20	○
17	FEM Tooth Profile Analysis	1.13	⊙
18	Rotational transmission error (Fourier analysis, Wow · flutter, CSV output)	1.16	⊙
19	Tooth surface evaluation (surface temp, film thickness, sliding velocity, PV value)	1.12	⊙
20	Tooth modification (involute, lead, bias)	1.14	⊙
21	Contact pattern	1.15	⊙

1.3 Property (Basic rack, accuracy, strength)

Setup screen is shown in Fig.1.2~1.5.

- gear combination : external × external, external × internal
- Basic rack : normal, low, special
- tooth tip circle decision : normal, equal clearance
- steel gear strength calculation spec is shown in Fig.1.5 as 3 types;
 - JGMA 401-02:1974, 402-02:1975
 - JGMA 6101-02:2007, 6102-02:2009
 - ISO6336:2006

Plastic strength calculation spec is JIS B 1759(2013).

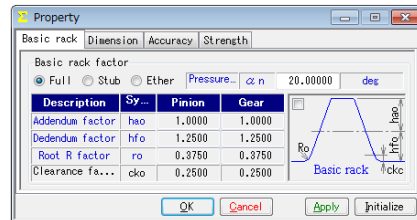


Fig.1.2 Basic rack

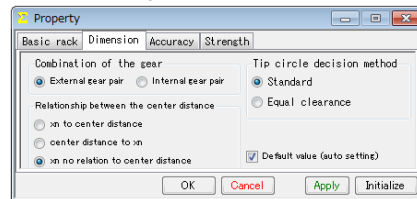


Fig.1.3 Dimension

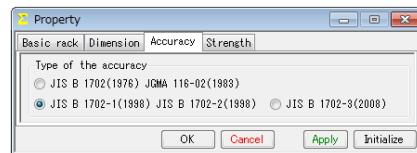


Fig.1.4 Accuracy

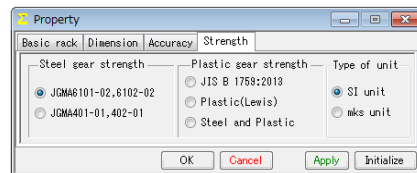


Fig.1.5 Strength

1.4 Dimension

Gear dimension calculates parts dimensions, contact ratio, sliding ratio, tooth thickness and so on. The gear with undercut determines the contact rate based on the TIF (True Involute Form) diameter. If tooth tip is rounded, R is considered in contact ratio.

(1)center distance and shift coefficient have the following 3 relationships.

<1> shift coefficient is given to pinion and gear to determine center distance.

<2> based on center distance, shift coefficient of each gear is determined.

<3> center distance is set, regardless of shift coefficient.

(2)shift coefficient is set per following 4 types;

<1>directly enter shift coefficient

<2>based on split tooth thickness, shift coefficient is set

<3>based on over pin dimension, shift coefficient is set

<4>based on arc tooth thickness, shift coefficient is set

Dimension setup screen is shown in Fig.1.6. Shift coefficient can be set by tooth thickness. See Fig.1.7 for dimension result.

Description	Sym	Unit	Pinion	Gear
Normal module	mn	mm	3.0000	
Number of teeth	z	---	22	33
Pressure angle	α_n	deg	20.0000	
Helix angle	β	deg	30 * 0	0.00
Helix directions	---	---	Right hand	Left hand
Reference diameter	d	mm	76.21024	114.31535
Base circle diameter	db	mm	70.25753	105.38630
Tooth thickness input ty...	---	---	xn	xn
Profile shift coefficient	xn	---	xn	0.12300
Number of teeth spanned	zm	---	zm & W dp & dm Sn	6
Span measurement	W	mm		51.04770
Measuring ball diameter	dp	mm	5.1046	5.0735
Measurement over balls	dm	mm	83.63825	121.73759
Normal circular tooth thi...	Sn	mm	4.93077	4.98100
Center distance	a	mm		96.00000
Tooth thinning for backla...	fn	mm	0.05000	0.06000
Face width	b	mm	23.00000	20.00000
Tip diameter	da	mm	82.81024	121.05335
Root diameter	df	mm	69.31024	107.55335
Tip radius	ra	mm	0.00000	0.00000
Root radius (Basic rack)	rf	mm	1.1250	1.1250

Fig.1.6 Dimension setup

Description	Sym	Unit	Pinion	Gear
Transverse module	mt	mm		3.46410
Transverse pressure angle	α_t	deg		22.79588
Effective face width	bw	mm		20.00000
Lead	pz	mm	414.69023	622.03595
Profile shift	Xm	mm	0.30000	0.36900
Addendum	ha	mm	3.30000	3.36900
Dedendum	hf	mm	3.45000	3.38100
Whole depth	h	mm	6.75000	6.75000
Clearance	c	mm	0.81821	0.81821
Base helix angle	β_b	deg	28 * 1	27.55
Operating transverse pressure a...	α_w	deg	23 * 49	15.64
Operating pitch diameter	dw	mm	76.80000	115.20000
Transverse circular pitch	pbt	mm		10.03275
Normal circular pitch	pbn	mm		8.85639
Contact length	ga	mm		12.92546
Transverse contact ratio	ϵ_c	---		1.28833
Overlap ratio	ϵ_β	---		1.06103
Total contact ratio	ϵ_γ	---		2.34936
Sliding ratio (tip side)	σ_a	---	0.48728	0.54712
Sliding ratio (root side)	σ_b	---	-1.20808	-0.95042
Span measurement (design)	W	mm	32.542672	50.967699
Measurement over balls (design)	dm	mm	83.571469	121.578627
Normal circular tooth thickness ...	sn	mm	4.877562	4.917148
Transverse tooth thickness (des...	st	mm	6.893564	5.751562
Transverse span measurement	Wa	mm	38.865179	57.760182
Chordal height	hj	mm	3.35381	3.40869
Chordal tooth thickness	Sj	mm	4.87578	4.91634
Basic rack addendum factor	hac	---	1.00000	1.00000
Basic rack dedendum factor	hfc	---	1.25000	1.25000
Backlash (transverse)	jt	mm		0.20737
Backlash (normal)	jn	mm		0.18429

Fig.1.7 Dimension result

1.5 Inference

For Inference-1, bending strength is used to set module and tooth width. Based on the estimated module and tooth width, next step of the design can be carried out. As there are multiple combinations of module/tooth width/material to satisfy strength, inference can be used to determine concept design.

For Inference-2, shift coefficient can be set based on sliding ratio and contact ratio. Fig.1.9 shows max sliding ratio for pinion in red line, gear in blue line, and contact ratio in green line. In Fig.1.9, the most suitable shift coefficient is 0.3 based on sliding ratio and contact ratio. Reasons for determining the shift coefficient are prevention of undercut, change of center distance, adjustment of meshing pressure angle, etc. However, by using this inference function, it is necessary to determine the shift coefficient based on the relationship between sliding ratio and contact ratio. When undercut is observed, sliding ratio will be large.

Description	Sym	Unit	Pinion	Gear
Gear material	---	---	S43C (N)HE20	
Heat treatment	---	---	normalizing	
Hardness	---	---	HE20	
Nominal stress num...	σ_{Flim}	MPa	205.3937	205.3937
Allowable stress num...	σ_{Hlim}	MPa	529.5591	529.5591
Torque	T	N·m	30.0000	75.0000
Rotational speed	n	rpm	1000.0000	400.0000
Module	mn	mm		1.5000
Number of teeth	z	---	20	50
Pressure angle	α_n	deg		20.00000
Helix angle	β	deg	20 * 0	0.00
Face width	b	mm		47.8880
Bending safety factor	SF	---		1.000
Circumference power	Fl	N		1879.3952
Allowable bending str...	σ_{FP}	MPa	307.8797	307.8797
Tooth bending stress	σ_F	MPa	30.0444	86.5319
Bending strength	Sft	---	3.3080	3.5555
Tooth surface damage...	SH	---		1.000
Circumference power	Fc	N		1879.3952
Allowable pitting stre...	σ_{HP}	MPa	628.1119	628.1119
Hertzian stress	σ_H	MPa	615.8360	615.8360
Pitting strength	Sfc	---	1.0203	1.0203

Fig.1.8 Inference-1 (Bending strength)

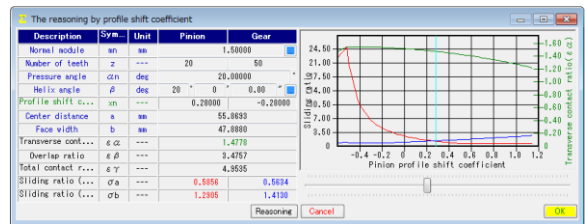


Fig.1.9 Inference-2 (Shift coefficient)

1.6 Tooth profile (Involute) drawing

Meshing drawing is shown in Fig.1.10. As shown in support form, zoom, distance measurement (Fig.1.11), R-measurement (Fig.1.12), diameter, involute modification, line of action, tooth tip width, odd teeth Y-measurement value display and rotation function are available. Involute creation is shown in Fig.1.13.

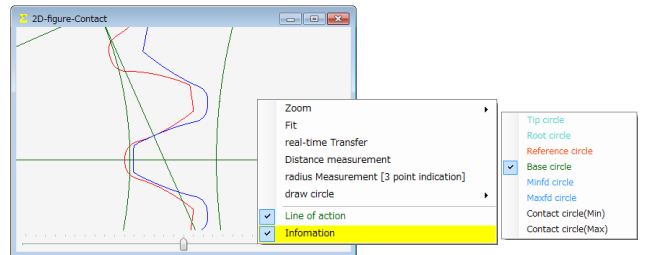


Fig.1.10 Meshing drawing & support form

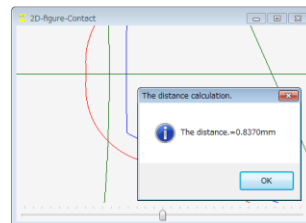


Fig.1.11 distance measurement

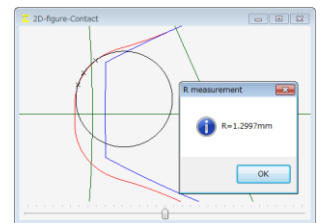


Fig.1.12 R measurement

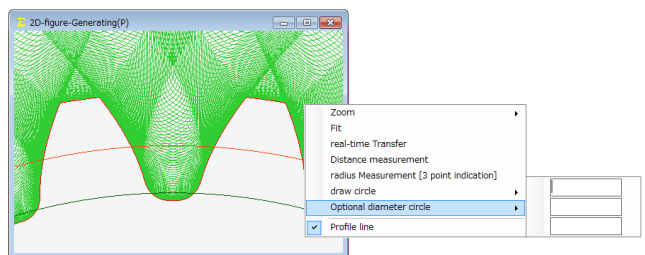


Fig.1.13 Involute creation (Pinion) & support form

1.7 Tooth profile rendering

3D tooth profile meshing can be created as shown in Fig.1.14, and contact line can be also observed. Control form allows the users to change tooth profile direction and size.

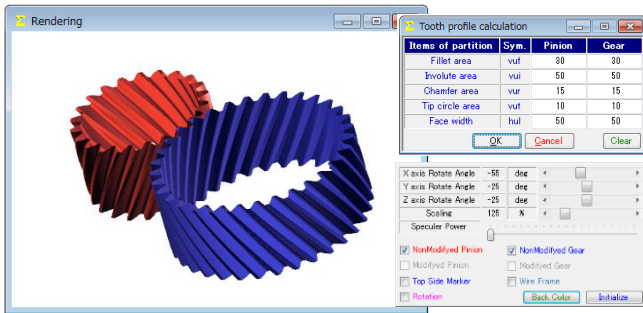


Fig.1.14 Tooth profile rendering

1.8 Gear accuracy

In Fig.1.15 & Fig.1.16, new JIS gear accuracy spec JIS B 1702-1:1998 and JIS B 1702-2:1998 are shown for tolerances. Also, New JIS and Old JIS can be switched as shown in Fig.1.4. Gear accuracy spec are 5 types as shown below;

- JIS B 1702-1:1998, JIS B 1702-2:1998, JIS B 1702-3:2008
- JIS B 1702:1976
- JGMA 116-02:1983

Description	Sym.	Unit	Pinion	Gear
Single pitch deviation	fst	μm	6	6
Cumulative pitch deviation	Fpk	μm	8.5	11
Total profile deviation	Fp	μm	10	10
Total helix deviation	Fβ	μm	8	8
Total helix deviation	Fβ	μm	10	10
Tooth-tooth tangential composite	f'1	μm	7.5	7.5
Total tangential deviation	F'1	μm	27	27
Profile form deviation	Ff	μm	6	6
Profile slope deviation	Hf	μm	5	5
Helix form deviation	Fβ	μm	7	7
Helix slope deviation	Hβ	μm	7	7

Fig.1.15 JIS B 1702-1

Description	Sym.	Unit	Pinion	Gear
Total radial composite deviat.	F1'	μm	25	25
Tooth-tooth radial composite	f1'	μm	10	10
Allowable radial runout	Fr	μm	15	15

Fig.1.16 JIS B 1702-2

1.9 Gear strength calculation(steel)

Gear strength calculation has several spec types as shown in Fig.1.5 for ISO6336:2006 based JGMA6101-02:2007 and JGMA 6102-02:2009 spec and JGMA401-01:1974, 402-01:1975. Design unit can be switched between SI and MKS unit. Strength calculation power setup menu is shown in Fig.1.17. Material selection is shown in Fig.1.18 for material and heat treatment. Bending coefficient setup menu is in Fig.1.19, stress coefficient setup menu in Fig.1.20, strength results are shown in Fig.1.21.

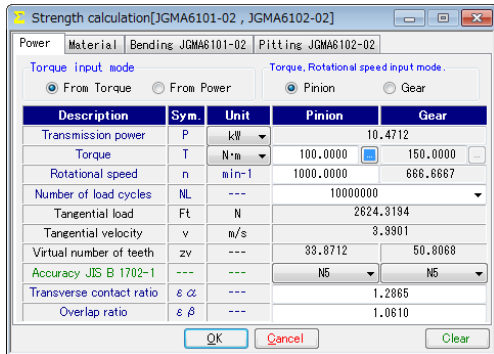


Fig.1.17 Strength calculation (Power setup)

1.10 Gear strength calculation(resin)

Plastic gear strength can be calculated by JIS B 1759(2013) or Lewis as shown by Fig.1.5. According to JIS B 1759 "Method for evaluating

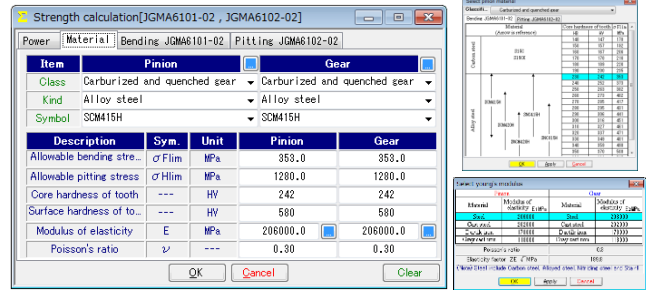


Fig.1.18 Strength calculation (material)

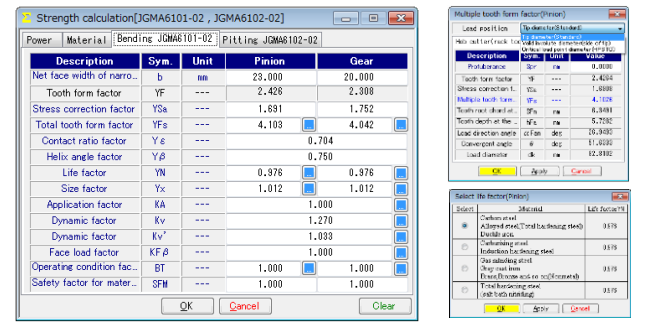


Fig.1.19 Strength calculation (bending coefficient)

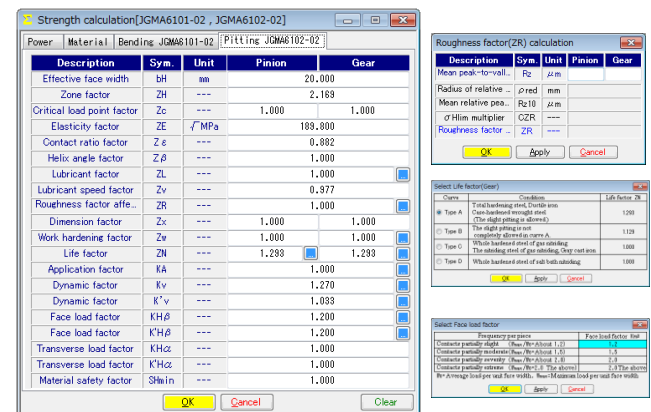


Fig.1.20 Strength calculation (stress coefficient)

Bending JGMA6101-02		Sym.	Unit	Pinion	Gear
Bending stress	σF	MPa		104.642	110.549
Allowable bending stress	σFP	MPa		522.394	522.394
General safety rate	SF	---		4.398	4.412
Allowable tangential force	Ft lim	N		18125.368	14233.673
Pitting JGMA6102-02		Sym.	Unit	Pinion	Gear
Hertzian stress	σH	MPa		753.325	753.325
Allowable pitting stress	σHP	MPa		1816.374	1816.374
General safety rate	SH	---		2.129	2.129
Allowable tangential force	Fci lim	N		14830.879	14830.879

Fig.1.21 Strength results

bending strength of plastic cylindrical gears", a method for determining the allowable bending stress of gears is based on testing, and POM allowable bending stress is set as 80.0[MPa] based on testing, and materials other than POM can be determined based on spec. Root bending stress and allowable root bending stress by considering each coefficient (root profile coefficient, life coefficient, ambient temperature coefficient etc) can be compared to determine the safety. Please see spec for details.

Plastic gear strength calculation example is shown in Fig.1.22, strength geometry is shown in Fig.1.23, bending stress is shown in Fig.1.24, spur gear equivalent value is shown in Fig.1.25, coefficient and safety factor are shown in Fig.1.26.

Setting of dimension				
Description	Sym	Unit	Pinion	Gear
Normal module	m	mm	1.00000	
Number of teeth	z	---	16	30
Pressure angle	α_n	deg	20.00000	
Helix angle	β	deg	20.00000	0.00000
Helix directions	---	---	Right hand	Left hand
Reference diameter	d	mm	17.02684	31.92533
Base circle diameter	db	mm	15.87745	29.77022
Tooth thickness type	---	---	xn	xn
Profile shift coefficient	xn	---	0.20000	0.12000
Number of teeth spanned	zm	---	3	5
Base tangent length	W	mm	7.78466	13.86829
Ball diameter	dp	mm	1.7705	1.7261
Over balls diameter	dm	mm	19.86949	34.54561
Circular tooth thickness	Sn	mm	1.71698	1.65815
Center distance	a	mm		24.90000
Tooth thinning for backla...	fn	mm	0.00000	0.00000
Face width	b	mm	10.00000	10.00000
Tip diameter	da	mm	19.42684	34.16533
Root diameter	df	mm	14.32684	29.66533
Tip radius	ra	mm	0.10000	0.10000
Basic rack root radius	rf	mm	0.3750	0.3750

Fig.1.22 Gear geometry

Bending strength of plastic gears JIS B 1759:2013				
Description	Sym	Unit	Pinion	Gear
Material	---	---		
Transmission power	P	W	52.9560	
Torque	T	N·m	0.5000	0.9375
Rotational speed	n	min ⁻¹	1000.0000	539.3393
Tangential load	F _t	N		57.7869
Tangential velocity	v _t	m/s		0.8070
Operating transverse pre...	α_{wt}	deg		23.56317
Transverse contact ratio	ϵ_{α}	---		1.2328
Number of load contact	N	---	10000000	5393393
Thickness of rim	s _r	mm	2.0000	2.0000
Allowable bending stress	σ_{Flim}	MPa	80.018	80.018
Tool tip radius	ρ_{FPv}	mm	0.3750	0.3750
Tooth form factor	Y _F	---	1.000	1.000
Life factor	Y _{NT}	---	0.779	0.829
Environment temperature...	Y _θ	---		1.000
Temperature rise factor	Y _{Δθ}	---		0.981
Lubricating factor	Y _L	---		1.190
Mating gear factor	Y _M	---		0.850
Minimum safety factor	S _{Fmin}	---	1.000	1.000

Fig.1.23 Strength geometry

Bending strength of plastic gears JIS B 1759:2013				
Description	Sym	Unit	Pinion	Gear
Bending stress	σ_F	MPa	18.033	17.853
Tooth form factor	Y _F	---	1.803	1.747
Basic rack root radius distance	E	mm	0.068	0.068
Auxiliary factor for critical se...	G	---	-0.675	-0.755
Auxiliary angle for critical sec...	H	rad	-0.888	-0.963
Generating angle of the tool	θ	rad	0.814	0.908
Critical section	S _{Fn}	mm	2.043	2.150
Bending moment arm	h _{Fe}	mm	1.265	1.340
Radius of root fillet	ρ_F	mm	0.504	0.499
Base helix angle	β_b	deg		18.74724

Fig.1.24 Root bending

Bending strength of plastic gears JIS B 1759:2013				
Description	Sym	Unit	Pinion	Gear
Number of teeth	zn	---	18.8882	35.6929
Transverse contact ratio	$\epsilon_{\alpha n}$	---		1.9748
Reference diameter	dn	mm	18.8882	35.6929
Normal circular pitch	p _{bn}	mm		2.9521
Base circle diameter	dbn	mm	17.8431	33.4559
Tip diameter	dasn	mm	21.3882	37.8429
Diameter (on HPSTC)	den	mm	20.2523	36.8986
Pressure angle (on HPSTC)	α_{en}	deg	28.23206	24.82018
Tooth angle (on HPSTC)	γ_e	deg	3.50208	1.84874
Work angle (on HPSTC)	α_{Fen}	deg	24.72988	22.97645

Fig.1.25 Equivalent spur gear

Bending strength of plastic gears JIS B 1759:2013				
Description	Sym	Unit	Pinion	Gear
Stress correction factor	Y _s	---	1.844	1.889
Function (s _{Fn} /h _{Fe})	L	---	1.815	1.804
Function (s _{Fn} /2p _F)	qs	---	2.027	2.156
Helix angle factor	Y _β	---		0.933
Rim thickness factor	Y _B	---	1.128	1.128
Back-up ratio	BR	---	0.889	0.889
Allowable bending stress	σ_{FP}	MPa	48.935	50.935
Safety factor for bending stre...	S _F	---	2.693	2.819
Safe judgement	---	---	S _F >S _{Fmin}	S _F >S _{Fmin}

Fig.1.26 Coefficient

1.11 Bearing load

Gear load and bearing load are calculated. Types of loads are tangential force, normal force and 20 loads on bearings are calculated as shown in Fig.1.27.

Bearing load				
Description	Sym	Unit	Pinion	Gear
Torque	T	N·m	100.0000	150.0000
Bearing span	p1, e1	mm	100.0000	100.0000
Bearing span	p2, e2	mm	100.0000	100.0000
Tangential load	F _t	N	2604.1667	
Normal load	F _n	N	3200.0173	
Radial load(Total)	F _r	N	1094.4704	
Axial load(Total)	F _a	N	1503.5163	
Radial load(Como)	F _{r11} , F _{r12}	N	1302.0893	1302.0893
Reference	OK	Cancel	Clear	

Fig.1.27 Bearing load

1.12 Gear surface evaluation

In surface evaluation, sliding ratio, Hertzian stress, film thickness, contact temperature, sliding speed, sliding speed drawing (PV value) are displayed. These are not used for tooth surface modification. Also, film thickness, contact temperature (gear temperature + flash temperature) are based on AGMA2001-C95, Annex A. Thus, for analysis by considering surface medication amount and load sharing, [45]CT-FEM Opera iii should be used. Oil types in Fig.1.28 can be Mineral oil, synthetic oil and ISO grade (customized setting is possible). In addition, the friction coefficient can be selected from a fixed value, ISO, AGMA method. Fig. 1.29 to 1.34 show the sliding ratio, Hertz stress graph, etc., but the horizontal scale can be switched between roll angle and line of action length.

Probability of occurrence of wear can be calculated from the oil film thickness in Fig.1.31, and the probability of scuffing from the contact temperature can be calculated as shown in Fig.1.32.

Tooth surface evaluation graph item				
Description	Symbol	Unit	Pinion	Gear
Gear temperature	G _{Tc}	°C		70.000
Oil temperature	T _c	°C		40.000
Kind of oil	---	---		Mineral oil
ISO viscosity grade	---	---		ISO VG 150
Kinematic viscosity at ...	---	mm ² /s		150
Average temperature	M _{Tc}	°C		227.000
Standard deviation tem...	SD	°C		37.000
Absolute viscosity	μ_0	cP		27.73
Pressure-viscosity	α	mm ² /N		0.01936
Roughness of tooth pla...	$\sigma_{1,2}$	μm	0.400	0.400
Method of friction coef...	---	---		constant value
Friction coefficient	μ_m	---		0.0800
Profile modification	---	---		Conducted
Driving member	---	---		Pinion
No. of calculation points	---	---		100

Fig.1.28 Surface evaluation (setup)

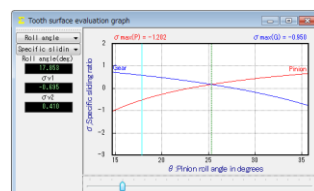


Fig.1.29 sliding ratio

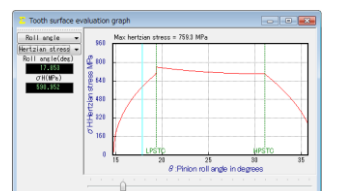


Fig.1.30 Hertz stress

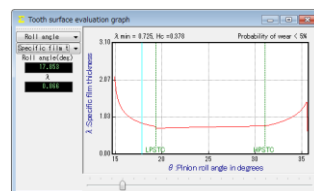


Fig.1.31 Film thickness

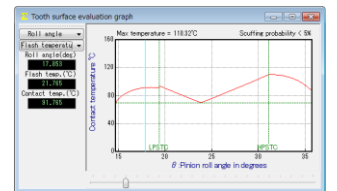


Fig.1.32 Flash temperature

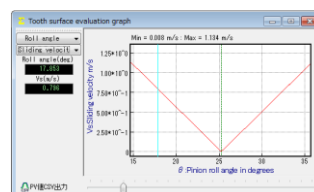


Fig.1.33 Sliding velocity

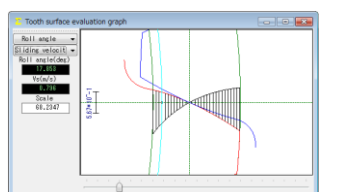


Fig.1.34 Sliding velocity drawing

1.12a Sliding ratio and Hertz stress graph

As involute tooth form, meshing pitch circle will be rolling motion, but others will involve slip motion. The example gear ($m_n=2, z_1=15, z_2=24, \alpha=20^\circ$ normal spur gear) in Fig.1.35 (left column) has sliding ratio, Hertzian stress, tooth surface contact temperature (gear temperature + flash temperature) and oil film thickness graph. Large Hertz stress change is observed in early meshing cycle due to pinion root sliding ratio. In this case, accuracy improvement would not help. In addition to contact ratio, sliding ratio and Hertz stress changes must be considered in design. To smooth out Hertz stress changes, shift coefficient medication may easily solve the challenge. It is important to consider sliding heat when designing resin gears.

When tooth modification (Smooth meshing) is carried out by using shift coefficient of $x_{n1}=0.24, x_{n2}=-0.24$ without changing center distance, sliding ratio, Hertz stress and tooth surface contact temperature changes are shown in Fig.1.36. As a result, scuffing probability is reduced from 59.4% in Fig.1.35(c) to 17.9% in Fig.1.36(c), while wear probability is reduced from 36% to 32%.

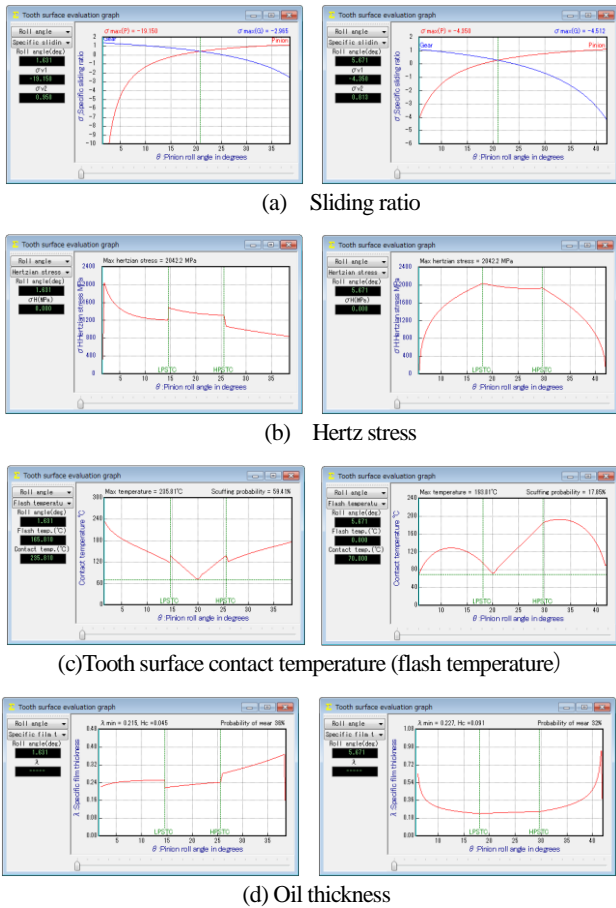


Fig.1.35 Normal gear

Fig.1.36 Shift coefficient

1.12b O class grade gear

Involute surface is as important as root shape. Involute testing result (both flank meshing) is shown in Fig.1.37 by connecting root curve with specific R. Also, theoretical trochoid curve involute test result is shown in Fig.1.38. Considering the creation motion as the basis, the root shape is a quasi-trochoid curve determined by (1) pressure angle, (2) basic rack root height, (3) basic rack root R, (4) shift amount, (5) number of teeth. involuteΣ iii (spur and helical) can output theoretical involute curve. Please see Appendix [D] for the effect of stress on the root shape.

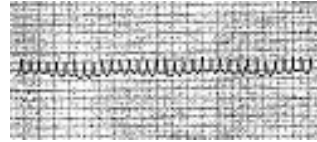


Fig.1.37 Gear test (specific R)

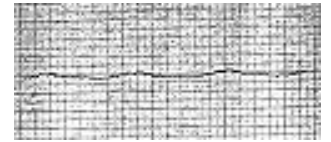


Fig.1.38 Gear test (theoretical involute)

1.13 FEM (Tooth profile stress analysis)

After strength analysis, clicking [FEM] icon allows the users to carry out stress analysis. FEM analysis setup screen is shown in Fig.1.39. By providing longitudinal elastic modulus, Poisson's ratio, number of partitions and load point position and load (changeable), stress ($\sigma_x, \sigma_y, \text{shear stress } \tau, \text{ main stress } \sigma_1, \sigma_2$) can be analyzed. Gear strength reliability can be improved by evaluating both gear strength and actual stress on teeth. Pinion max main stress σ_1 distribution is shown in Fig. 1.40. Tooth profile displacement (contour display is possible) and involute modification amount is shown in Fig.1.41.

Tooth profile modification is a useful method for improving driving performance of gears, so even if the gears are accurate, the difference in normal pitch occurs between the teeth of the drive and the driven gears due to deflection of teeth at the time of meshing. Mismatch due to this difference in normal pitch causes [vibration] and [sound]. Tooth profile modification is one way to solve this. Since displacement of small elastic modulus like resin material increases, it can be said that the tooth profile modification effect is even greater. As shown in Fig.41, it is possible to know the amount of deflection of teeth when determining tooth tip modification by 2D-FEM, determination of 3D tooth surface modification requires [45] CT - FEM Opera iii.

FEM analysis item				
Description	Sym.	Unit	Pinion	Gear
Method of analysis	---	---	2D-FEM stress analysis	
Material symbol	---	---	SCM415H	SCM415H
Elastic modulus	E	MPa	206000.0	206000.0
Poisson's ratio	ν	---	0.30	0.30
No. of partitions(depth)	nD	---	21	21
No. of partitions(width)	nW	---	21	21
Position of the load point	Nf	---	2	2
Load	F	N	2624.3194	

Fig.1.39 FEM setup (2D)

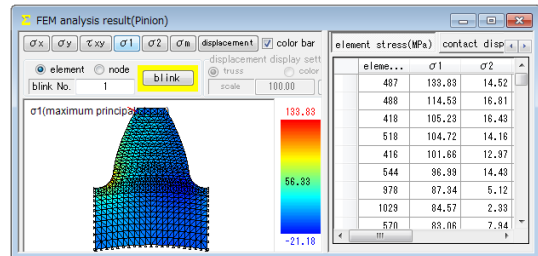


Fig.1.40 Max main stress σ_1 (Pinion)

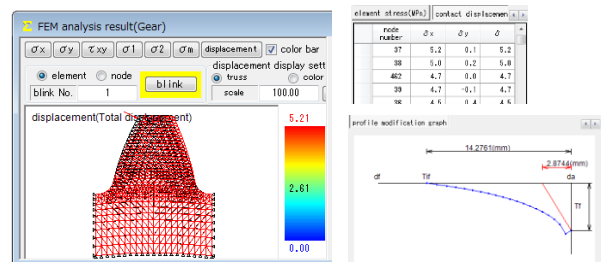


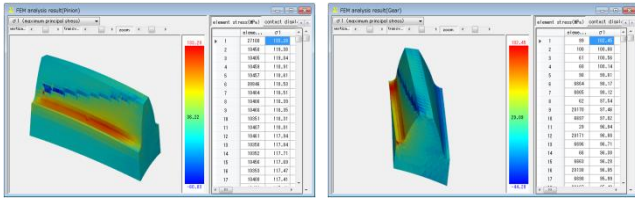
Fig.1.41 Tooth displacement & graph (Gear)

Fig.1.42 shows 3D-FEM analysis condition setting screen. Fig.1.43 shows pinion and gear stress distribution, and Fig.1.44 shows pinion and gear displacement. Also, observation angle can be changed by vertical rotation and horizontal rotation function with the scroll bar at the top of the screen in Fig.1.43 and Fig.1.44, and the figure can be enlarged or reduced with zoom function.

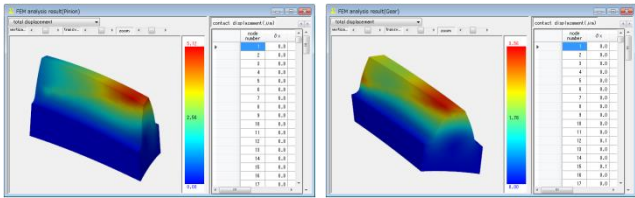
In this software, stress and displacement of the tooth is calculated when a load acts on one tooth. However, stress, tooth displacement, axial angle error, tooth profile error, pitch error, and tooth surface modification need to be considered when load is applied to multiple simultaneous meshing teeth, please use [45]CT-FEM Opera iii.

Description	Sym	Unit	Pinion	Gear
Method of analysis				
Material symbol	---	---	SCM415H	SCM415H
Elastic modulus	E	MPa	208000.0	208000.0
Poisson's ratio	ν	---	0.30	0.30
No. of partitions(depth)	nD	---	11	11
No. of partitions(width)	wD	---	11	11
Position of the load point	NF	---	2	2
Load	F	N		2624.3194

Fig.1.42 FEM setup (3D)



(a)Pinion (b)Gear
Fig.1.43 Max main stress σ_1



(a)Pinion (b)Gear
Fig.1.44 Tooth displacement

1.14 Gear modification (involute, lead, bias)

Fig.1.45 shows an example of giving tooth surface modification. In order to obtain this tooth form, it is possible to give tooth profile modification by numerical input as shown in Fig.1.46, or it can be done by inputting a numerical value to patterned tooth form as shown on the right side. Likewise, lead modification can also be set as shown in Fig. 1.47.

The tooth profile modification and lead modification represented in Fig.1.48 can be copied on the opposite tooth surface for identical tooth profile as shown in Fig.1.45. In addition, "involute", "lead", "involute/lead" in the combo box at the top of the screen in Fig.1.48 can be selected, and involute height direction can be assigned by line of action or diameter. In addition, the magnification of tooth profile modification can be set up to 1000 times.

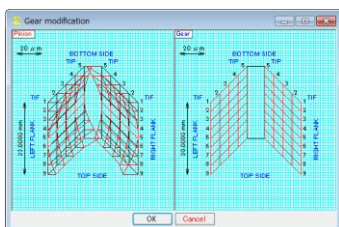


Fig.1.45 Tooth surface modification (Topo graph)

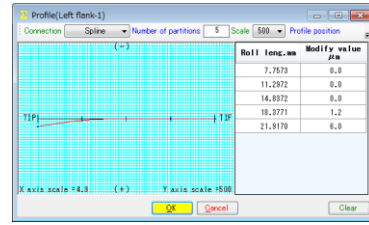


Fig.1.46 Involute modification

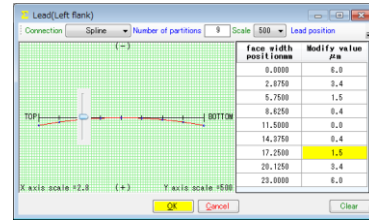


Fig.1.47 Lead modification

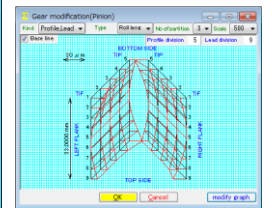
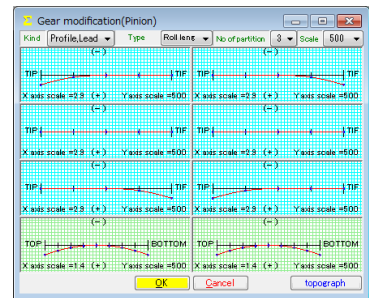


Fig.1.48 Involute & Lead modification & Topo graph

Modified tooth profile can be set with the tooth profile calculation data in Fig.1.49. The tooth profile calculation conditions set here are valid for the tooth form shown in Fig.1.10 to 1.14 and can be superimposed on the tooth form rendering of Fig.1.14, so it can be displayed as shown in Fig. 1.50. Here, since tooth surface modification is given to Pinion, a yellow tooth surface appears within the red tooth surface in the figure (Gear is unmodified).

Items of partition	Sym	Pinion	Gear
Fillet area	vuf	30	30
Involute area	vui	50	50
Chamfer area	zur	15	15
Tip circle area	vut	10	10
Face width	hul	31	31

Fig.1.49 Tooth calculation dimension

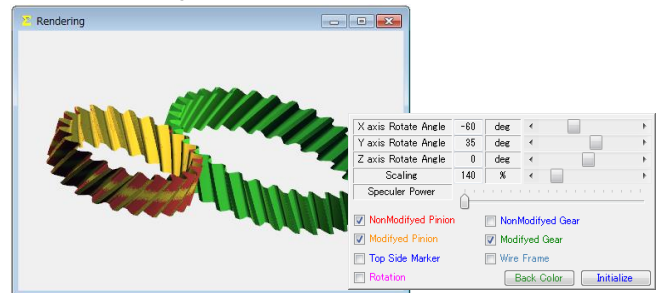


Fig.1.50 Tooth rendering (tooth modification)

1.15 Contact pattern

It is possible to check the tooth contact by setting the tooth contact condition in Fig.1.51 on the gear given the tooth surface modification (Fig.1.45). Here, the tooth contact is shown in Fig.1.52 and Fig.1.53

when parallelism error and discrepancy error are 0 and the contact maximum clearance is 2.0 μm .

Teeth contact analysis item			
Description	Sym.	Unit	Value
Center distance	a	mm	98.0000
Parallelism error	p	deg	0.00000
Discrepancy error	d1	deg	0.00000
Lead division number	hul	---	20
Interpolation accuracy	ac	μm	0.0
No. of division of rotation(Pe...	urP	---	50
Contact maximum clearance	c	μm	3.0
Direction of rotation			
<input checked="" type="radio"/> Both faces <input type="radio"/> CCW(Left face) <input type="radio"/> CW(Right face)			
<input type="button" value="OK"/> <input type="button" value="Cancel"/> <input type="button" value="Clear"/>			

Fig.1.51 Contact setup

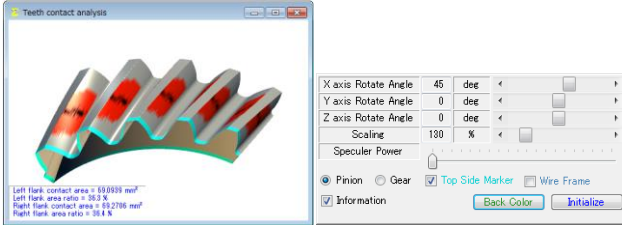


Fig.1.52 Contact pattern (Pinion)

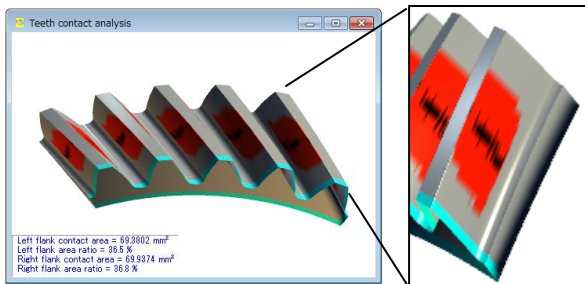
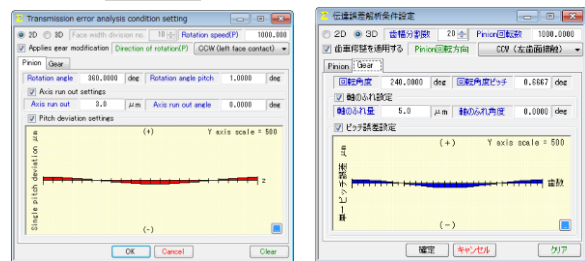


Fig.1.53 Contact pattern (Gear) & magnified

1.16 Transmission error (TE) analysis

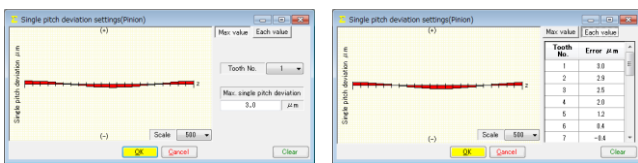
In TE analysis, it is possible to perform a rotation transmission error test under no load with a non-modified tooth profile or the tooth profile given in Fig.1.45. The TE setting is shown in Fig.1.54. In this case, 2D analysis or 3D analysis can be selected, and axis runout and rotation speed can be set. As for pitch error, maximum value or pitch error of all teeth can be set as shown in Fig.1.55. TE analysis, wow flutter (rotation irregularity) and Fourier analysis results are shown in Fig. 1.56 to 1.58. In Fig. 1.57 [Sound] can be heard.



(a)Pinion

(b)Gear

Fig.1.54 TE setup



(a) Max value setup

(b) All teeth setup

Fig.1.55 Pitch error setup

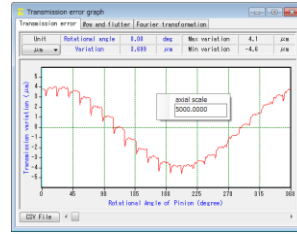


Fig.1.56 TE result

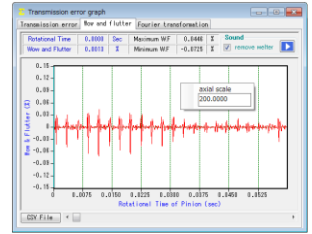


Fig.1.57 Wow flutter

TE analysis, Wow flutter, Fourier analysis results can be output to csv file (361 pieces of data in this example) as shown in Fig.1.59 in the lower left corner of Fig.1.56 ~ 1.58 [CSV File]

This software is a TE analysis test with no load. For TE analysis corresponding to load and shaft angle error, please use [45]CT-FEM Operaⁱⁱⁱ.

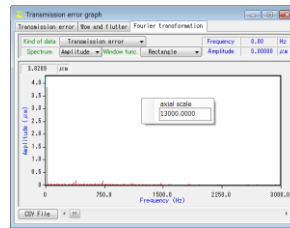


Fig.1.58 Fourier analysis

F3		
	A	B
1	0	3.69856E
2	1	3.75217E
3	2	3.80616E
4	3	3.79174
5	4	3.66043E
6	5	3.74891E
7	6	3.077734
8	7	3.5500E
9	8	3.731161

Fig.1.59 csv file example

1.17 Tooth profile output

The generated tooth profile can be output in the tooth profile file format shown in Fig.1.60. In the case of 3D-IGES, it is possible to select integrated type and separated type of tooth profile,

In the case of a separated type, it is split into a root fillet part, involute tooth surface, tooth tip R, and a tooth tip, and then output as shown in Fig. 1.61. In the coordinate correction setting shown in Fig.1.62, it is possible to output tooth profile considering the module shrinkage rate, pressure angle correction, helix angle correction, and discharge gap in consideration of use for molds. As an example, Fig.1.63 shows a tooth profile (2D) considering the module shrinkage factor of 20/1000. Also, it is possible to output the tooth profile coordinate value as a text file as shown in Fig.1.64.

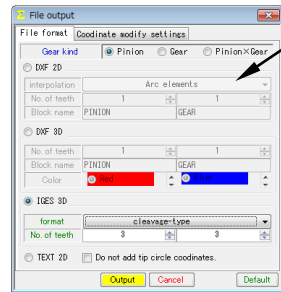


Fig.1.60 Tooth file format

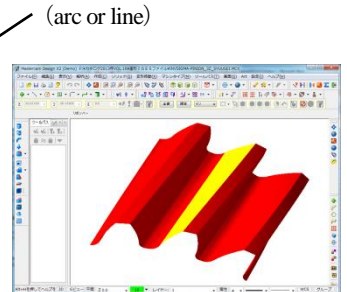


Fig.1.61 CAD sample

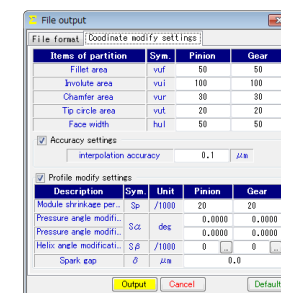


Fig.1.62 Coordinate correction setup

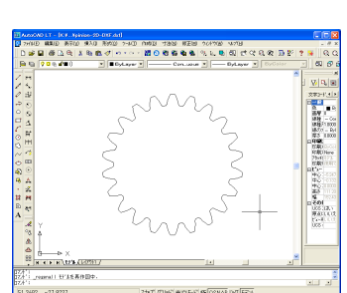


Fig.1.63 CAD sample

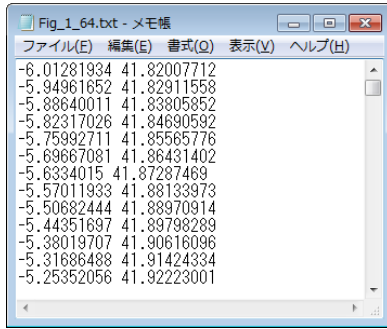


Fig.1.64 Text file (.txt)

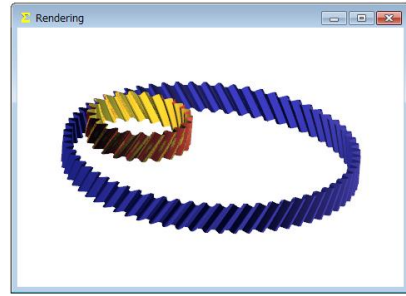


Fig.1.67 Rendering

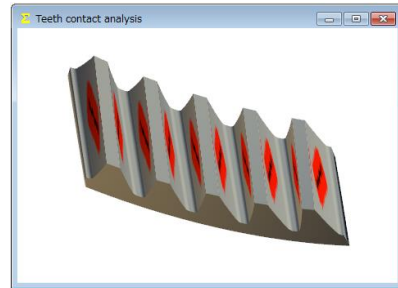


Fig.1.68 Contact pattern (Gear)

1.18 Internal gear

Internal gear can be calculated like External gear by selecting "External gear × Internal gear" in Fig.1.3. Fig.1.65 shows concept dimensions, while Fig.1.66 shows detail dimensions. Fig.1.67 shows tooth profile rendering while Fig.1.68 shows tooth contact pattern. In addition, Pinion that meshes with Gear in Fig.1.68 is given the same tooth surface modification as Fig.1.45. Strength calculation, TE analysis, FEM analysis and tooth profile output are the same as "External gear × External gear".

Setting of dimension				
Description	Sym.	Unit	Pinion	Gear
Normal module	m	mm		3.00000
Number of teeth	z	---	22	65
Pressure angle	α_n	deg		20.00000
Helix angle	β	deg	30 * 0	0.00
Helix directions	---	---	Right hand	Right hand
Reference diameter	d	mm	76.21024	225.16680
Base circle diameter	db	mm	70.25753	207.57907
Tooth thickness type	---	---	xn	
Profile shift coefficient	xn	---	0.10000	0.12300
Number of teeth spanned	zm	---	4	11
Base tangent length	W	mm	32.59267	97.35180
Ball diameter	dp	mm	5.0000	5.0000
Over balls diameter	dm	mm	83.32747	219.15583
Circular tooth thickness	Sn	mm	4.38077	4.44378
Center distance	a	mm		74.54701
Tooth thinning for backla...	fn	mm	0.05000	0.06000
Face width	b	mm	23.00000	23.00000
Tip diameter	da	mm	82.81024	219.30460
Root diameter	df	mm	69.31024	233.40480
Tip radius	ra	mm	0.10000	0.10000
Basic rack root radius	rf	mm	1.1250	1.1250

Fig.1.65 Concept dimension (Internal gear)

Dimension result				
Description	Sym.	Unit	Pinion	Gear
Transverse module	mt	mm		3.46410
Transverse pressure angle	α_t	deg		22.79588
Effective face width	bv	mm		23.00000
Lead	pz	mm	414.69023	1225.22113
Profile shift	Xm	mm	0.30000	0.36800
Addendum	ha	mm	3.30000	2.63100
Dedendum	hf	mm	3.45000	4.11800
Whole depth	h	mm	6.75000	6.75000
Clearance	c	mm	0.75017	0.75017
Base helix angle	β_b	deg	28 * 1	27.55
Operative transverse pressure a...	α_w	deg	22 * 55	17.09
Operative pitch diameter	dw	mm	76.28068	225.37468
Transverse circular pitch	pbt	mm		10.03275
Normal circular pitch	pbn	mm		8.85639
Contact length	ga	mm		14.05211
Transverse contact ratio	ϵ_z	---		1.40082
Overlap ratio	ϵ_β	---		1.22019
Total contact ratio	ϵ_γ	---		2.62081
Sliding ratio (tip side)	σ_a	---	0.21134	0.37589
Sliding ratio (root side)	σ_b	---	-0.60227	-0.26797
Span measurement (design)	W	mm	32.542672	97.411804
Over balls diameter(design)	dm	mm	83.198909	219.335224
Circular tooth thickness (design)	sn	mm	4.877562	4.379928
Transverse tooth thickness (des...	st	mm	5.63564	5.131234
Transverse span measurement	Ws	mm	36.865179	110.350381
Chordal height	hj	mm	3.35981	2.62037
Chordal tooth thickness	Sj	mm	4.87578	4.36891
Basic rack addendum factor	ha0	---	1.00000	1.00000
Basic rack dedendum factor	hf0	---	1.25000	1.25000
Backlash (transverse)	j_t	mm		0.13529
Backlash (normal)	j_n	mm		0.10791
Contact circle diameter(Min)	dca	mm	82.71581	220.24702
Contact circle diameter(Max)	dca	mm	71.95802	231.16852

Fig.1.66 Detail dimension (internal gear)

1.19 HELP feature

[HELP] function can be used to understand the operation method. For example, if the user wants to know about gear accuracy, by activating the "Precision" form and press the [F1] key, the explanation about accuracy is displayed as shown in Fig.1.69.

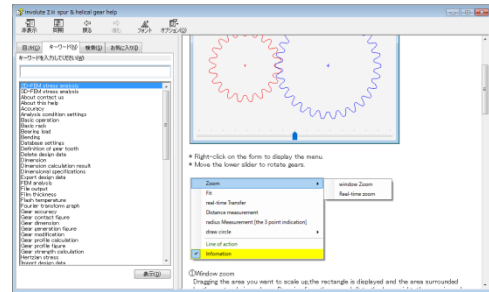


Fig.1.69 HELP function

1.20 Design data management (Saving / Loading)

The design data can be saved and loaded as shown in Fig.1.70. In addition to the control number and the title, users can also retrieve the data from the gear specification (module, number of teeth, pressure angle, helix angle).

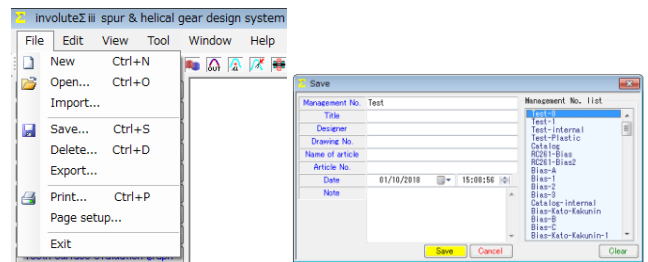


Fig.1.70 Data saving, loading